## Fairfield Township School Year-long Curricular Framework Mathematics - Grade 8


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## Fairfield Township School Year-long Curricular Framework Mathematics - Grade 8




## 8.G.B.8 Finding the distance between points

8.EE.C. 8 Kimi and Jordan

MP. 8 Look for and express regularity in repeated reasoning.

| 21st Century Life and Careers Career Awareness, Exploration, and Preparation | 9.2.12.C.1 Review career goals and determine steps necessary for attainment. <br> 9.2.12.C. 2 Modify Personalized Student Learning Plans to support declared career goals <br> 9.2.12.C. 3 Identify transferable career skills and design alternate career plans. <br> 9.2.12.C.6 Investigate entrepreneurship opportunities as options for career planning and identify the knowledge, skills, abilities, and resources required for owning and managing a business. <br> 9.2.12.C. 9 Analyze the correlation between personal and financial behavior and employability |
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| CRP Standards | CRP1. Act as a responsible and contributing citizen and employee. <br> CRP2. Apply appropriate academic and technical skills. <br> CRP7. Employ valid and reliable research strategies. <br> CRP8. Utilize critical thinking to make sense of problems and persevere in solving them. <br> CRP10. Plan education and career paths aligned to personal goals. <br> CRP11. Use technology to enhance productivity. <br> CRP12. Work productively in teams while using cultural global competence |
| ELA Standards | RI.8.1. Cite the textual evidence and make relevant connections that most strongly supports an analysis of what the text says explicitly as well as inferences drawn from the text. <br> RI.8.4. Determine the meaning of words and phrases as they are used in a text, including figurative, connotative, and technical meanings; analyze the impact of specific word choices on meaning and tone, including analogies or allusions to other texts. <br> W.8.4. Produce clear and coherent writing in which the development, organization, voice and style are appropriate to task, purpose, and audience. <br> SL.8.4. Present claims and findings, emphasizing salient points in a focused, coherent manner with relevant evidence, sound valid reasoning, and well-chosen |
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|  | details; use appropriate eye contact, adequate volume, and clear pronunciation. |
| :--- | :--- |
| Technology Standards | 8.1.8.A.3 Use and/or develop a simulation that provides an environment to solve a <br> real world problem or theory |
|  | 8.1.8.C.1 Collaborate to develop and publish work that provides perspectives on a <br> global problem for discussions with learners from other countries. <br>  <br>  <br>  <br>  <br>  <br>  <br>  <br>  <br>  <br>  <br> 8.1.8.D.5 Understand appropriate uses for social media and the negative <br> 8.1.8.E.1 Effectively use a variety of search tools and filters in professional public <br> databases to find information to solve a real world problem. <br> 8.1.8.F.1 Explore a local issue, by using digital tools to collect and analyze data to <br> identify a solution and make an informed decision. |


| Unit 1 Grade 8 - Exponents, Expressions, Equations, scientific notation |  |  |
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| Content Standards | Suggested Standards for Mathematical Practice | Transfer |
| - 8.EE.A.1. Know and apply the properties of integer exponents to generate equivalent numerical expressions. For example, $3^{2} \times 3^{-5}=$ $3^{-3}=1 / 3^{3}=1 / 27$. <br> - 8.G.C.9. Know the formulas for the volumes of cones, cylinders, and spheres and use them to solve realworld and mathematical problems. | MP. 1 Make sense of problems and persevere in solving them. <br> MP. 2 Reason abstractly and quantitatively. <br> MP. 4 Model with mathematics. <br> MP. 5 Use appropriate tools | Concept(s): <br> - Exponents as simplified representation of repeated multiplication. <br> Students are able to: <br> - apply properties of exponents to numerical expressions. <br> - generate equivalent numerical expressions using positive and negative integer exponents. <br> - find volume of cones, cylinders and spheres using to solve real world problems. |
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|  | strategically. <br> MP. 6 Attend to precision. <br> MP. 7 Look for and make use of structure. <br> MP. 8 Look for and express regularity in repeated reasoning. | Learning Goal 1: Apply the properties of integer exponents to write equivalent numerical expressions; apply formulas to find the volume of a cone, a cylinder, or a sphere when solving real-world and mathematical problems. |
| :---: | :---: | :---: |
| - 8.EE.A.3. Use numbers expressed in the form of a single digit times an integer power of 10 to estimate very large or very small quantities, and to express how many times as much one is than the other. For example, estimate the population of the United States as $3 \times 10^{8}$ and the population of the world as $7 \times 10^{9}$, and determine that the world population is more than 20 times larger. | MP. 2 Reason abstractly and quantitatively. <br> MP. 4 Model with mathematics. <br> MP. 5 Use appropriate tools strategically. <br> MP. 6 Attend to precision. <br> MP. 7 Look for and make use of structure. <br> MP. 8 Look for and express regularity in repeated reasoning. | Concept(s): <br> - Very large and very small quantities can be approximated with numbers expressed in the form of a single digit times an integer power of 10 . <br> Students are able to: <br> - estimate very large and very small quantities with numbers expressed in the form of a single digit times an integer power of 10 . <br> - compare numbers written in the form of a single digit times an integer power of 10 and express how many times as much one is than the other. <br> Learning Goal 2: Estimate and express the values of very large or very small numbers with numbers expressed in the form of a single digit times an integer power of 10. Compare numbers expressed in this form, expressing how many times larger or smaller one is than the other. |
| - 8.EE.A.4. Perform operations with numbers expressed in scientific notation, including problems where both decimal and scientific notation are used. Use scientific notation and choose units of appropriate size for measurements of very large or very small quantities (e.g., use millimeters per year for seafloor spreading). Interpret scientific notation that has been generated by technology. | MP. 2 Reason abstractly and quantitatively. <br> MP. 4 Model with mathematics. <br> MP. 5 Use appropriate tools strategically. <br> MP. 6 Attend to precision. <br> MP. 7 Look for and make use of | Concept(s): No new concept(s) introduced <br> Students are able to: <br> - multiply and divide numbers expressed in scientific notation, including problems in which one number is in decimal form and one is in scientific notation. <br> - add and subtract numbers expressed in scientific notation, including problems in which one number is in decimal form and one is in scientific notation. <br> - use scientific notation and choose units of appropriate size for measurements of very large or very small quantities. |
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|  | structure. <br> MP. 8 Look for and express regularity in repeated reasoning. | - interpret scientific notation that has been generated by technology (e.g. recognize $4.1 \mathrm{E}-2$ and $4.1 \mathrm{e}-2$ as $4.1 \times 10^{-2}$ ). <br> Learning Goal 3: Perform operations using numbers expressed in scientific notation, including problems where both decimals and scientific notation are used. In real-world problem-solving situations, choose units of appropriate size for measurement of very small and very large quantities and interpret scientific notation generated when technology has been used for calculations. |
| :---: | :---: | :---: |
| - 8.NS.A.1. Know that numbers that are not rational are called irrational. Understand informally that every number has a decimal expansion; for rational numbers show that the decimal expansion repeats eventually, and convert a decimal expansion which repeats eventually into a rational number. | MP. 2 Reason abstractly and quantitatively. | Concept(s): <br> - Numbers that are not rational are irrational. <br> - Every number has a decimal expansion. <br> Students are able to: <br> - compare decimal expansions of rational and irrational numbers. <br> - represent a rational number with its decimal expansion, showing that it repeats eventually. <br> - convert a decimal expansion (which repeats eventually) into a rational number. <br> Learning Goal 4: Represent a rational number with its decimal expansion, showing that it eventually repeats, and convert such decimal expansions into rational numbers. |
| - 8.NS.A.2. Use rational approximations of irrational numbers to compare the size of irrational numbers, locate them approximately on a number line diagram, and estimate the value of expressions (e.g., $\square^{2}$ ). For example, by truncating the decimal expansion of 2 , show that 2 is between 1 and 2 , then between 1.4 and 1.5 , and explain how to continue on to get better approximations. | MP. 1 Make sense of problems and persevere in solving them. <br> MP. 4 Model with mathematics. <br> MP. 5 Use appropriate tools strategically. | Concept(s): <br> - Rational approximation of irrational numbers <br> Students are able to: <br> - compare irrational numbers by replacing each with its rational approximation. <br> - locate rational approximations on a number line. <br> - estimate the value of expressions containing irrational numbers. <br> Learning Goal 5: Use rational numbers to approximate irrational numbers, locate |
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|  |  | irrational numbers on a number line, and estimate the value of expressions containing irrational numbers. |
| :---: | :---: | :---: |
| - 8.EE.B.5. Graph proportional relationships, interpreting the unit rate as the slope of the graph. Compare two different proportional relationships represented in different ways. For example, compare a distance-time graph to a distance-time equation to determine which of two moving objects has greater speed. | MP. 2 Reason abstractly and quantitatively. <br> MP. 4 Model with mathematics. <br> MP. 5 Use appropriate tools strategically. MP. 6 Attend to precision. <br> MP. 7 Look for and make use of structure. <br> MP. 8 Look for and express regularity in repeated reasoning. | Concept(s): <br> - Quantitative relationships can be represented in different ways. <br> Students are able to: <br> - graph proportional relationships. <br> - interpret unit rate as the slope of a graph. <br> - compare two different proportional relationships that are represented indifferent ways (table of values, equation, graph, verbal description). <br> Learning Goal 6: Graph proportional relationships, interpreting slope as unit rate, and compare two proportional relationships, each represented in different ways. |
| - 8.EE.B.6. Use similar triangles to explain why the slope $m$ is the same between any two distinct points on a non-vertical line in the coordinate plane; derive the equation $y=m x$ for a line through the origin and the equation $y=m x+b$ for a line intercepting the vertical axis at $b$. | MP. 2 Reason abstractly and quantitatively. <br> MP. 4 Model with mathematics. <br> MP. 5 Use appropriate tools strategically. <br> MP. 6 Attend to precision. <br> MP. 7 Look for and make use of structure. <br> MP. 8 Look for and express regularity in repeated reasoning. | Concept(s): No new concept(s) introduced <br> Students are able to: <br> - show, using similar triangles, and explain why the slope, $m$, is the same between any two distinct points on a non-vertical line. <br> - derive, from two points, the equation $y=m x$ for a line through the origin. <br> - derive, from two points, the equation $y=m x+b$ for a line intercepting the vertical axis at $b$. <br> Learning Goal 7: Derive the equation of a line ( $y=m x$ for a line through the origin and the equation $y=m x+b$ for a line intercepting the vertical axis at $b$ ) and use similar triangles to explain why the slope ( $m$ ) is the same between any two points on a non-vertical line in the coordinate plane. |


| District/School Formative Assessment Plan | District/School Summative Assessment Plan |
| :---: | :---: |
| $\bullet$ Teacher-Created Assessments | $\bullet$ Chapter Tests |

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- Homework
- Classwork
- UDL's
- whiteboard activities
- IXL
- Problem of the Day
- Exit Ticket
- Unit Tests
- EdConnect Assessments

Focus Mathematical Concepts

| Vocabulary |  | Instruction and Pacing |  |
| :---: | :---: | :---: | :---: |
|  |  | Pretest | 1 day |
|  |  | Exponents | 1 week |
| Rational Number |  | Scientific notation | 1 week |
| Irrational number |  | Rational/Irrational numbers | 1 week |
| Terminating decimal | Coefficient | Graphing on a number line | 1 week |
| Repeating Decimal Integer | Variable Substitute | Unit rate | 1 week |
| Absolute Value | Unit rate | Unit rate as slope | 2 weeks |
| Exponent | Slope | Similar triangles and slope | 2 weeks |
| Scientific Notation Standard Form power | Similar Triangles |  |  |

## ENDURING UNDERSTANDING

- Models, diagrams, manipulatives and patterns are useful in developing and remembering algorithms for computing with positive and negative rational numbers.
- Properties of real numbers hold for all rational numbers.
- Positive and negative rational numbers are often used to solve problems in everyday life.
- An irrational number is a real number that cannot be written as a ratio of


## ESSENTIAL QUESTIONS

- What properties will help me simplify and evaluate rational numbers?
- How can rational numbers be applied to solve real-world situations?
- When are exponents used and why are they important?
- What is the meaning of negative exponents?
- How are power, base, and exponent related to multiplication?
- Why is it useful for me to express quantities in scientific notation?
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two integers.
- All real numbers can be plotted on a number line.
- Exponents are useful for representing very large or very small numbers.


## Differentiation and Accommodations

- Provide graphic organizers
- Provide additional examples and opportunities for additional problems

> District/School Primary and Supplementary Resources
for repetition

- IXL
- Teacher created materials
- Provide tutoring opportunities
- Provide retesting opportunities after remediation (up to teacher and district discretion)
- Teach for mastery not test
- Teaching concepts in different modalities
- Adjust pace and homework assignments


## Instructional Strategies

Fairfield Township School recognizes the importance of the varying methodologies that may be successfully employed by teachers within the classroom and, as a result, identifies a wide variety of possible instructional strategies that may be used effectively to support student achievement. These may include, but not be limited to, strategies that fall into categories identified by the Framework for Teaching by Charlotte Danielson:

- Communicating with students
- Using questioning and discussion techniques
- Engaging students in learning
- Using assessment in instruction
- Demonstrating Flexibility and Responsiveness

Common Misconceptions

| Common Misconceptions | Proper Conceptions |
| :--- | :--- |
| When converting a fraction to a decimal, the numerator is the divisor. | When converting a fraction to a decimal, the numerator is the dividend. | Negative exponents yield a negative answer. Zero as an exponent equals zero.

Negative exponents yield an answer that is a fraction
Zero as an exponent always equals 1.
Performance Task

## DISTANCE FROM THE SUN IN MILES




Use the data in the chart above to make a new chart listing the distance each planet is from the sun in scientific notation. Rubric: Quiz grade worth 10 pts each.

| Unit 2 Grade 8 - Functions, equations, and solutions |  |  |  |
| :---: | :---: | :---: | :---: |
| Content Standards | Suggested Standards for Mathematical Practice |  | Transfer |
| - 8.F.A.1. Understand that a function is a rule that assigns to each input exactly one output. The graph of a function is the set of ordered pairs consisting of an input and the corresponding output. | MP. 2 Reason abstractly and quantitatively. <br> MP. 5 Use appropriate tools strategically. |  | Concept(s): <br> - A function is a rule. <br> - If a rule is a function, then for each input there is exactly one output. <br> Students are able to: <br> - use function language. <br> - describe a function as providing a single output for each input. |
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|  |  | - determine whether non-numerical relationships are functions. <br> - describe a function as a set of ordered pairs. <br> - read inputs and outputs from a graph. <br> - describe the ordered pairs as containing an input, and the corresponding output. <br> Learning Goal 1: Define a function as a rule that assigns one output to each input and determine if data represented as a graph or in a table is a function. |
| :---: | :---: | :---: |
| - 8.F.A.2. Compare properties (e.g. rate of change, intercepts, domain and range) of two functions each represented in a different way (algebraically, graphically, numerically in tables, or by verbal descriptions). For example, given a linear function represented by a table of values and a linear function represented by an algebraic expression, determine which function has the greater rate of change. | MP. 5 Use appropriate tools strategically. MP. 8 Look for and express regularity in repeated reasoning. | Concept(s): <br> - Functions (quantitative relationships) can be represented in different ways. <br> - Functions have properties; properties of linear functions. <br> Students are able to: <br> - analyze functions represented algebraically, as a table of values, and as a graph. <br> - interpret functions represented by a verbal description. <br> - given two functions, each represented in a different way, compare their properties. <br> Learning Goal 2: Compare two functions each represented in a different way (numerically, verbally, graphically, and algebraically) and draw conclusions about their properties (rate of change and intercepts). |
| - 8.F.A. 3 Interpret the equation $y=$ $m x+b$ as defining a linear function, whose graph is a straight line; give examples of functions that are not linear. For example, the function $A=$ $s^{2}$ giving the area of a square as a function of its side length is not linear because its graph contains the points $(1,1),(2,4)$ and $(3,9)$, which are not on a straight line. | MP. 2 Reason abstractly and quantitatively. <br> MP. 3 Construct viable arguments and critique the reasoning of others. <br> MP. 5 Use appropriate tools strategically. | Concept(s): <br> - A linear function is defined by the equation $y=m x+b$. <br> - The graph of a linear function is a straight line. <br> Students are able to: <br> - analyze tables of values, graphs, and equations in order to classify a function as linear or non-linear. <br> - determine if equations presented in forms other than $\mathrm{y}=\mathrm{mx}+\mathrm{b}$ (for example $3 y-2 x=7$ ) define a linear function. <br> - give examples of equations that are non-linear functions. <br> - show that a function is not linear using pairs of points. |
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|  |  | Learning Goal 3: Classify functions as linear or non-linear by analyzing equations, graphs, and tables of values; interpret the equation $y=m x+b$ as defining a linear function. |
| :---: | :---: | :---: |
| - 8.F.B.4. Construct a function to model a linear relationship between two quantities. Determine the rate of change and initial value of the function from a description of a relationship or from two $(x, y)$ values, including reading these from a table or from a graph. Interpret the rate of change and initial value of a linear function in terms of the situation it models, and in terms of its graph or a table of values. | MP. 6 Attend to precision. <br> MP. 2 Reason abstractly and quantitatively. <br> MP. 7 Look for and make use of structure. | Concept(s): <br> - As with equations, two ( $\mathrm{x}, \mathrm{y}$ ) values can be used to construct a function. <br> Students are able to: <br> - determine the rate of change and initial value of a function from a description of a relationship. <br> - determine the rate of change and initial value of a function from two ( $x, y$ ) values by reading from a table of values. <br> - determine the rate of change and initial value of a function from two $(x, y)$ values by reading these from a graph. <br> - construct a function in order to model a linear relationship. <br> - interpret the rate of change and initial value of a linear function in context. <br> Learning Goal 4: Model a linear relationship by constructing a function from two ( $\mathrm{x}, \mathrm{y}$ ) values. Interpret the rate of change and initial value of the linear function in terms of the situation it models, and in terms of its graph or a table of values. |
| - 8.F.B.5. Describe qualitatively the functional relationship between two quantities by analyzing a graph (e.g., where the function is increasing or decreasing, linear or nonlinear). Sketch a graph that exhibits the qualitative features of a function that has been described verbally. | MP. 1 Make sense of problems and persevere in solving them. <br> MP. 2 Reason abstractly and quantitatively. <br> MP. 4 Model with mathematics. <br> MP. 5 Use appropriate tools strategically. | Concept(s): No new concept(s) introduced <br> Students are able to: <br> - analyze a graph. <br> - provide qualitative descriptions of graphs (e.g. where increasing or decreasing, linear or non-linear). <br> - given a verbal description, sketch a graph of a function based on the qualitative features described. <br> Learning Goal 5: Sketch a graph of a function from a qualitative description and give a qualitative description of a graph of a function. |
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- 8.EE.C.7. Solve linear equations in one variable.

8EE.C.7a. Give examples of linear equations in one variable with one solution, infinitely many solutions, or no solutions. Show which of these possibilities is the case by successively transforming the given equation into simpler forms, until an equivalent equation of the form $x=a, a=$ $a$, or $a=b$ results (where $a$ and $b$ are different numbers). 8.EE.C.7b. Solve linear equations with rational number coefficients, including equations whose solutions require expanding expressions using the distributive property and collecting like terms.

MP. 5 Use appropriate tools strategically.

MP. 6 Attend to precision.

Concept(s):

- Linear equations may have an infinite number of solutions.
- Linear equations may have no solution or a single solution.

Students are able to:

- give examples of linear equations in one variable with one solution $(x=a)$, infinitely many solutions ( $a=a$ ), or no solutions ( $a=b$.)
- transform a given equation, using the properties of equality, into simpler forms.
- transform a given equation until an equivalent equation of the form $x=a, a=$ $a$, or $a=b$ results ( $a$ and $b$ are different numbers).
- solve linear equations that have fractional coefficients; include equations requiring use of the distributive property and collecting like terms.

Learning Goal 6: Apply the distributive property and collect like terms to solve linear equations in one variable that contain rational numbers as coefficients. Use an equivalent equation of the form $x=a, a=a$, or $a=$ $b$ (where $a$ and $b$ are different numbers) to describe the number of solutions.

## Concept(s):

- Simultaneous linear equations may have an infinite number of solutions.
- Simultaneous linear equations may have no solution or a single solution.
- Solutions to a system of two linear equations in two variables correspond to points of intersection of their graphs.
Students will be able to:
- solve systems of two linear equations in two variables algebraically.
- estimate solutions of a linear system of two equations by graphing.
- solve simple cases of a linear system of two equations by inspection.
- solve real-world and mathematical problems leading to two linear equations in two variables. the equations. Solve simple cases by inspection. For
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example, $3 x+2 y=5$ and $3 x+2 y$ $=6$ have no solution because $3 x$
$+2 y$ cannot simultaneously be 5 and 6.
8.EE.C.8c. Solve real-world and mathematical problems leading to two linear equations in two variables. For example, given coordinates for two pairs of points, determine whether the line through the first pair of points intersects the line through the second pair.

Learning Goal 7: Solve systems of linear equations in two variables algebraically and by inspection. Estimate solutions by graphing, explain that points of intersection satisfy both equations simultaneously, and interpret solutions in context.

District/School Formative Assessment Plan

- Teacher-Created Assessments
- Homework
- Classwork
- UDL's
- whiteboard activities
- IXL
- Problem of the Day
- Exit Ticket

Focus Mathematical Concepts

## District/School Summative Assessment Plan

- Chapter Tests
- Unit Tests
- EdConnect Assessments


## Vocabulary

Equation
Expression
Variable
Instruction and Pacing

| Pretest | 1 day |
| :--- | :--- |
| Function tables | 1 week |
| Graphing functions | 1 week |
| Linear functions | 1 week |
| Slope | 1 week |

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## One step/two step/multi step equations

Distributive property
Inverse operations
Like terms
Function
Linear function
Slope
System of equations
solutions

## ENDURING UNDERSTANDING

- Systems of equations can be solved both graphically and algebraically
- There are situations that require two or more equations to be satisfied simultaneously.
- Some word problems can be solved using two variables or only one variable.
- Solutions to systems can be interpreted algebraically, geometrically, and in terms of problem contexts.
- The number of solutions to a system of equations can vary from no solution to an infinite number of solutions.
- An algebraic expression is variables and numbers combined by operations and can be represented by equivalent forms (such as combining like terms).
- The properties of real numbers are true for algebraic as well as numeric expressions.
- Expressions can be written using numeric values or variables.
- Relations show any correspondence between sets, while functions show predictable relations between sets.
- Linear functions are defined by constant slope.
- Written descriptions, tables, graphs, and equations are useful in representing and investigating relationships between varying quantities.

| Equations | 1 week |
| :--- | :--- |
| Equations with distributive property | 2 weeks |
| System of equations | 2 weeks |
|  |  |
|  |  |
| ESSENTIAL QUESTIONS |  |

- How do you decide which method would be easier to use for finding the solution for a system of equations?
- How can you use systems of equations to solve real-world problems and interpret the results?
- How does an algebraic solution differ from a graphic solution in a real-life situation?
- How can I interpret the meaning of a "system of equations" algebraically and geometrically?
- How does mathematical notation indicate that equations are to be treated as a system?
- What does it mean to solve a system of linear equations?
- How can the solution to a system be interpreted geometrically?
- How can I recognize how many solutions a system of equations has prior to solving?
- How can I translate a problem situation into a system of equations?
- What does the solution to a system tell me about the answer to a problem situation?
- What is an algebraic expression?
- How are various properties used in order to simplify, evaluate, and expand algebraic expressions?
- Are there other forms of expressions that can illustrate the problem?
- How can I determine the rule that produces the output from the given input?
- How can I identify a function?
- How can I tell the difference between a relation and a function?
- Which tells me more about the relationship I am investigating - a table, a graph, or an equation? Why?

> Differentiation and Accommodations

District/School Primary and Supplementary Resources

- Provide graphic organizers
- Provide additional examples and opportunities for additional problems for repetition
- Provide tutoring opportunities
- Provide retesting opportunities after remediation (up to teacher and district discretion)
- Teach for mastery not test
- Teaching concepts in different modalities
- Adjust pace and homework assignments
- Prentice Hall Course 3 Mathematics Common Core Textbook
- IXL
- Teacher created materials
Instructional Strategies

Fairfield Township School recognizes the importance of the varying methodologies that may be successfully employed by teachers within the classroom and, as a result, identifies a wide variety of possible instructional strategies that may be used effectively to support student achievement. These may include, but not be limited to, strategies that fall into categories identified by the Framework for Teaching by Charlotte Danielson:

- Communicating with students
- Using questioning and discussion techniques
- Engaging students in learning
- Using assessment in instruction
- Demonstrating Flexibility and Responsiveness


## Common Misconceptions

## Proper Conceptions

Students confuse whether to add/subtract or multiply/divide first when solving 2- $\quad$ Add/subtract first; multiply/divide second
step equations
Students get confused when combining like terms $\quad$ Only combine terms that have the same variable
Students get confused when moving a term from one side of the equal sign to the $\quad$ Be aware of the terms' sign before moving it (using inverse operation) other

## Performance Task

Tracey has two paintings in her portfolio and paints three more each week. Lisa has twelve paintings in her portfolio and paints two more each week. After how many weeks will Tracey and Lisa have the same number of paintings?

- Write an equation to represent the situation.
- Solve the equation.
- Work must be shown.
- Explain how you used inverse operations to solve the equation.


## Rubric

## When used as a quiz grade (based on $100 \%$ ), each bullet would be worth 25 points for a correct answer.

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| Unit 3 Grade 8 Pythagorean Theorem, transformations |  |  |
| :---: | :---: | :---: |
| Content Standards | Suggested Standards for Mathematical Practice | Transfer |
| - 8.EE.A.2. Use square root and cube root symbols to represent solutions to equations of the form $x^{2}=p$ and $x^{3}=p$, where $p$ is a positive rational number. Evaluate square roots of small perfect squares and cube roots of small perfect cubes. Know that 2 is irrational. <br> - 8.G.C.9. Know the formulas for the volumes of cones, cylinders, and spheres and use them to solve realworld and mathematical problems. | MP. 2 Reason abstractly and quantitatively. <br> MP. 4 Model with mathematics. <br> MP. 5 Use appropriate tools strategically. <br> MP. 6 Attend to precision. <br> MP. 7 Look for and make use of structure. <br> MP. 8 Look for and express regularity in repeated reasoning. | Concept(s): <br> - Square root and cube roots; perfect squares and perfect cubes <br> - Inverse relationship between powers and square roots <br> Students are able to: <br> - give the value of square roots of small perfect squares. <br> - solve equations of the form $x^{2}=p$, where $p$ is a positive rational number. <br> - use the square root symbol to represent solutions to equations of the form $x^{2}$ $=p$. <br> - give the value of cube roots of small perfect cubes. <br> - solve equations of the form $x^{3}=p$, where $p$ is a positive rational number. <br> - use the cube root symbol to represent solutions to equations of the form $x^{3}=$ $p$. <br> - show or explain that 2 is an irrational number. |

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|  |  | of right triangles in two and three dimensional cases when solving real-world and mathematical problems. |
| :---: | :---: | :---: |
| - 8.G.B.8. Apply the Pythagorean Theorem to find the distance between two points in a coordinate system | MP. 2 Reason abstractly and quantitatively. <br> MP. 7 Look for and make use of structure. | Concept(s): No new concept(s) introduced <br> Students are able to: <br> - determine the distance between two points in a coordinate plane by drawing a right triangle and applying the Pythagorean Theorem. <br> Learning Goal 5: Use the Pythagorean Theorem to determine the distance between two points in the coordinate plane. |
| - 8.G.A.1. Verify experimentally the properties of rotations, reflections, and translations: <br> 8.G.A.1a. Lines are transformed to lines, and line segments to line segments of the same length. <br> 8.G.A.1b. Angles are transformed to angles of the same measure. <br> 8.G.A.1c. Parallel lines are transformed to parallel lines. | MP. 3 Construct viable arguments and critique the reasoning of others. <br> MP. 5 Use appropriate tools strategically. <br> MP. 8 Look for and express regularity in repeated reasoning. | Concept(s): <br> - A property of rigid motion transformations (rotation, reflection, and translation) is that the measure of a two-dimensional object under the transformation remains unchanged. <br> Students are able to: <br> - show and explain that performing rotations, reflections, and translations on lines results in a line. <br> - show and explain that performing rotations, reflections, and translations on line segments results in a line segment and does not alter the length of the line segment. <br> - show and explain that performing rotations, reflections, and translations on angles results in an angle and does not alter the measure of the angle. <br> - show and explain that performing rotations, reflections, and translations on parallel lines results in parallel lines. <br> - explain that a property of rigid motion transformations (rotation, reflection, and translation) is that the measure of a two-dimensional object under the transformation remains unchanged. <br> Learning Goal 6: Explain and model the properties of rotations, reflections, and translations with physical representations and/or geometry software using pre-images and resultant images of lines, line |

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|  |  | segments, and angles. |
| :---: | :---: | :---: |
| - 8.G.A.2. Understand that a twodimensional figure is congruent to another if the second can be obtained from the first by a sequence of rotations, reflections, and translations; given two congruent figures, describe a sequence that exhibits the congruence between them. | MP. 2 Reason abstractly and quantitatively. <br> MP. 7 Look for and make use of structure. | Concept(s): <br> - A two-dimensional figure is congruent to another if the second can be obtained from the first by a sequence of rotations, reflections, and translations. <br> Students are able to: <br> - given two congruent figures, describe a transformation or sequence of transformations that shows the congruence between them. <br> Learning Goal 7: Describe and perform a sequence of rotations, reflections, and/or translations on a two dimensional figure in order to prove that two figures are congruent. |
| - 8.G.A.3. Describe the effect of dilations, translations, rotations, and reflections on two-dimensional figures using coordinates. | MP. 2 Reason abstractly and quantitatively. <br> MP. 3 Construct viable arguments and critique the reasoning. of others. <br> MP. 5 Use appropriate tools strategically. | Concept(s): No new concept(s) introduced <br> Students are able to: <br> - describe, using coordinates, the resulting two-dimensional figure after applying dilations with scale factor greater than, less than, and equal to 1. <br> - describe, using coordinates, the resulting two-dimensional figure after applying translation, rotation, and reflection. <br> Learning Goal 8: Use the coordinate plane to locate images or pre-images of twodimensional figures and determine the coordinates of a resultant image after applying dilations, rotations, reflections, and translations. |
| - 8.G.A.4. Understand that a twodimensional figure is similar to another if the second can be obtained from the first by a sequence of rotations, reflections, translations, and dilations; given two similar two-dimensional figures, describe a sequence that | MP. 2 Reason abstractly and quantitatively. <br> MP. 7 Look for and make use of structure. | Concept(s): <br> - A two-dimensional figure is similar to another if the second can be obtained from the first by a sequence of rotations, reflections, translations, and dilations. <br> - Congruent figures are also similar. |

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exhibits the similarity between them.
8.G.A. 5 Use informal arguments to establish facts about the angle sum and exterior angle of triangles, about the angles created when parallel lines are cut by a transversal, and the angle-angle criterion for similarity of triangles. example, arrange three copies of the same triangle so that the sum of the three angles appears to form a line, and give an argument in terms of transversals why this is so.

Students are able to:

- describe a transformation or sequence of transformations that show the similarity between them given two similar two-dimensional figures.

Learning Goal 9: Apply an effective sequence of transformations to determine that figures are similar when corresponding angles are congruent and corresponding sides are proportional. Write similarity statements based on such transformations.

Concept(s): No new concept(s) introduced
Students are able to:

- give informal arguments to establish facts about the angle sum of triangles.
- give informal arguments to establish facts about exterior angles of triangles.
- give informal arguments to establish facts about the angles created when parallel lines are cut by a transversal.
- give informal arguments to establish the angle-angle criterion for similarity of triangles.

Learning Goal 10: Give informal arguments to justify facts about the exterior angles of a triangle, the sum of the measures of the interior angles of a triangle, the angle-angle relationship used to determine similar triangles, and the angles created when parallel lines are cut by a transversal.

## District/School Formative Assessment Plan

- Teacher-Created Assessments
- Homework
- Classwork
- UDL's
- whiteboard activities
- IXL
- Problem of the Day
- Exit Ticket

Focus Mathematical Concepts

| Vocabulary |  | Instruction and Pacing |  |
| :---: | :---: | :---: | :---: |
|  | Similar Figures | Pretest | 1 day |
|  | Complementary Angles | Square roots \& cube roots | 1 week |
| Coordinate Plane | Supplementary Angles | Volume of 3-d figures | 2 weeks |
| Axes | Vertical Angles | Pythagorean Theorem | 2 weeks |
| Origin | Corresponding Angles | Transformations | 2 weeks |
| Quadrant Horizontal | Alternate Interior Angles | Angles | 2 weeks |
| Vertical | Alternate Exterior Angles |  |  |
| Translation | Square root |  |  |
| Reflection | Cube root |  |  |
| Rotation | Leg |  |  |
| Dilation | Hypotenuse |  |  |
| Proportion |  |  |  |

## ENDURING UNDERSTANDING

- Use two-dimensional figure is congruent to another if the second can be obtained by a series of transformations.
- Transformations of a two-dimensional figure on the coordinate plane will involve a change in coordinates.
- Dilation is a transformation that changes the size of a figure, but not the shape.
- If the second figure can be obtained from the first by a sequence of transformations, they are similar.
- Use informal arguments to establish facts about the angle sum and exterior angles of triangles, about the angles created when parallel lines are cut by a transversal, and the angle-angle relationship used to identify similar triangles.
- There are many relationships between the lengths of the sides of a right
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| triangle. |  |
| :---: | :---: |
| Differentiation and Accommodations | District/School Primary and Supplementary Resources |
| - Provide graphic organizers <br> - Provide additional examples and opportunities for additional problems for repetition <br> - Provide tutoring opportunities <br> - Provide retesting opportunities after remediation (up to teacher and district discretion) <br> - Teach for mastery not test <br> - Teaching concepts in different modalities <br> - Adjust pace and homework assignments | - Prentice Hall Course 3 Mathematics Common Core Textbook <br> - IXL <br> - Teacher created materials |
| Instructional Strategies |  |
| Fairfield Township School recognizes the importance of the varying methodologies identifies a wide variety of possible instructional strategies that may be used effective strategies that fall into categories identified by the Framework for Teaching by Cha <br> - Communicating with students <br> - Using questioning and discussion techniques <br> - Engaging students in learning <br> - Using assessment in instruction <br> - Demonstrating Flexibility and Responsiveness | hat may be successfully employed by teachers within the classroom and, as a result, ly to support student achievement. These may include, but not be limited to, tte Danielson: |
| Common Misconceptions | Proper Conceptions |
| To find the leg (a) of a right triangle, you square side $b$ and $c$ and add their values | To find the leg (a) of a right triangle, you square side $b$ and $c$ and subtract their values. |
| Complementary angles have a sum of 90 degrees, not 180 degrees. | Complementary angles have a sum of 90 degrees. |
| Supplementary angles have a sum of 180 degrees, not 90 degrees. | Supplementary angles have a sum of 180 degrees. |
| Performance Task |  |
| $\Delta A B C$ has coordinates $A(1,2), B(2,5)$, and $C(3,1)$. <br> - On a coordinate plane, graph $\triangle \mathrm{ABC}$ and its image after a translation 6 <br> - On the same coordinate plane, graph the image of $\Delta A^{\prime} B^{\prime} C^{\prime}$ after a refle <br> - On the same coordinate plane, graph the image of $\Delta A$ " $B^{\prime \prime} C^{\prime \prime}$ after a rot <br> - Explain the difference between a translation, a reflection, and a rotat | nits to the left. ion over the x-axis. ion of $90^{\circ}$ about the origin. . |

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## Rubric : When used as a quiz grade (based on $100 \%$ ), each bullet would be worth 25 points for a correct answer.

| Unit 4 Grade 8 - Statistics and Probability ; review linear functions/slope \& system of equations |  |  |
| :---: | :---: | :---: |
| Content Standards | Suggested Standards for Mathematical Practice | Transfer |
| - 8.SP.A.1. Construct and interpret scatter plots for bivariate measurement data to investigate patterns of association between two quantities. Describe patterns such as clustering, outliers, positive or negative association, linear association, and nonlinear association. | MP. 3 Construct viable arguments and critique the reasoning. of others. <br> MP. 5 Use appropriate tools strategically. <br> MP. 7 Look for and make use of structure. | Concept(s): <br> - Association in data (bivariate measurement data) <br> Students are able to: <br> - construct and interpret scatter plots. <br> - analyze patterns of association between the two quantities represented in a scatter plot. <br> - describe clustering, outliers, positive or negative association, linear or non-linear association when explaining patterns of association in a scatter plot. <br> Learning Goal 1: Construct and interpret scatter plots for bivariate measurement data and describe visual patterns of association (clusters, outliers, positive or negative association, linear association and nonlinear association, strong, weak, and no association). |
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- 8.SP.A.2. Know that straight lines are widely used to model relationships between two quantitative variables. For scatter plots that suggest a linear association, informally fit a straight line, and informally assess the model fit (e.g. line of best fit) by judging the closeness of the data points to the line.
- 8.SP.A.3. Use the equation of a linear model to solve problems in the context of bivariate measurement data, interpreting the slope and intercept. For example, in a linear model for a biology experiment, interpret a slope of 1.5 $\mathrm{cm} / \mathrm{hr}$ as meaning that an additional hour of sunlight each day is associated with an additional 1.5 cm in mature plant height.
- 8.SP.A.4. Understand that patterns of association can also be seen in bivariate categorical data by displaying frequencies and relative frequencies in a two-way table. Construct and interpret a two-way table summarizing data on two categorical variables collected from the same subjects. Use relative frequencies calculated for rows or columns to describe possible

MP. 2 Reason abstractly and quantitatively.

MP. 5 Use appropriate tools strategically.
MP. 7 Look for and make use of structure.

MP. 2 Reason abstractly and quantitatively.

MP. 4 Model with mathematics.
MP. 6 Attend to precision.
MP. 7 Look for and make use of structure. quantitatively.

MP. 4 Model with mathematics.
MP. 5 Use appropriate tools strategically.

MP. 7 Look for and make use of structure.

Concept(s):

- Straight lines are used to model approximately linear relationships between quantitative variables.
Students are able to:
- informally fit a line (of best fit) to a scatter plot that suggests a linear association.
- informally assess the model's fit by judging the closeness of the data points to the line (line of best fit).

Learning Goal 2: For scatter plots that suggest a linear association, informally fit a straight line and informally assess the model's fit.

Concept(s): No new concept(s) introduced
Students are able to:

- given the equation for a linear model (line of best fit), interpret the slope and intercept.
- given the equation for a linear model, solve problems in the context of measurement data.

Learning Goal 3: Use a linear model (equation) representing measurement data to solve problems, interpreting the slope and intercept in the context of the situation.

## Concept(s):

- Categorical data: patterns of association can also be observed in bivariate categorical data through analyzing two-way tables containing frequencies or relative frequencies.
Students are able to:
- construct and interpret a two-way frequency table containing data on two categorical variables.
- construct and interpret a two-way relative frequency table containing data
association between the two
variables. For example, collect data from students in your class on whether or not they have a curfew on school nights and whether or not they have assigned chores at home. Is there evidence that those who have a curfew also tend to have chores?
- 8.F.B.4. Construct a function to model a linear relationship between two quantities. Determine the rate of change and initial value of the function from a description of a relationship or from two $(x, y)$ values, including reading these from a table or from a graph. Interpret the rate of change and initial value of a linear function in terms of the situation it models, and in terms of its graph or a table of values.
- 8.G.B.7. Apply the Pythagorean Theorem to determine unknown side lengths in right triangles in real-world and mathematical problems in two and three dimensions.
- 8.G.B.8. Apply the Pythagorean Theorem to find the distance between two points in a coordinate system.


## on two categorical variables.

- describe any association between the two categorical variables using relative frequencies calculated for rows or columns.

Learning Goal 4: Construct two-way frequency tables and two-way relative frequency tables, and describe possible associations between two variables.

## MP. 2 Reason abstractly and

 quantitatively.MP. 6 Attend to precision.
MP. 7 Look for and make use of structure.

Concept(s):

- As with equations, two $(x, y)$ values can be used to construct a function. Students are able to:
- construct a function in order to model a linear relationship.
- interpret the rate of change and initial value of a linear function in context.

Learning Goal 5: Model a linear relationship by constructing a function from two $(x, y)$ values. Interpret the rate of change and initial value of the linear function in terms of the situation it models, and in terms of its graph or a table of values.

## MP. 2 Reason abstractly and

 quantitatively.MP. 7 Look for and make use of structure.

Concept(s): No new concept(s) introduced
Students are able to:

- determine side lengths of right triangles by applying the Pythagorean Theorem to solve real world and mathematical problems in two and three dimensions.
- determine the distance between two points in a coordinate plane by applying the Pythagorean Theorem.

Learning Goal 6: Apply the Pythagorean Theorem to determine unknown side lengths of right triangles in two and three dimensions to solve real-world and mathematical problems and to determine the distance between two points in the coordinate plane.

| - 8.EE.C.8. Analyze and solve pairs of simultaneous linear equations. 8.EE.C.8c. Solve real-world and mathematical problems leading to two linear equations in two variables. For example, given coordinates for two pairs of points, determine whether the line through the first pair of points intersects the line through the second pair. | MP. 2 Reason abstractly and quantitatively. <br> MP. 6 Attend to precision. <br> MP. 1 Make sense of problems and persevere in solving them. MP. 7 Look for and make use of structure. | Concept(s): <br> - Simultaneous linear equations may have an infinite number of solutions. <br> - Simultaneous linear equations may have no solution or a single solution. <br> - Solutions to a system of two linear equations in two variables correspond to points of intersection of their graphs. <br> Students will be able to: <br> - solve systems of two linear equations in two variables algebraically. <br> - estimate solutions of a linear system of two equations by graphing. <br> - solve simple cases of a linear system of two equations by inspection. <br> - solve real-world and mathematical problems leading to two linear equations in two variables. <br> Learning Goal 7: Solve real world and mathematical problems leading to two linear equations in two variables, interpreting solutions in context. |
| :---: | :---: | :---: |


| District/School Formative Assessment Plan | District/School Summative Assessment Plan |
| :---: | :---: |
| - Teacher-Created Assessments <br> - Homework <br> - Classwork <br> - UDL's <br> - whiteboard activities <br> - IXL <br> - Problem of the Day <br> - Exit Ticket | - Chapter Tests <br> - Unit Tests <br> - EdConnect Assessments |

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| Focus Mathematical Concepts |  |  |  |
| :---: | :---: | :---: | :---: |
| Vocabulary |  | Instruction and Pacing |  |
| Frequency table <br> Scatter plot <br> Correlation/ Trend (Positive, negative, none) <br> Line of best fit <br> Slope <br> Function <br> Pythagorean theorem <br> System of equations |  | Pretest | 1 day |
|  |  | Scatterplot | 1 week |
|  |  | Line of best fit in scatterplots | 1 week |
|  |  | Slope of line of best fit | 1 week |
|  |  | Frequency tables | 1 week |
|  |  | Review functions | 1 week |
|  |  | Review Pythagorean theorem Review system of equations | 1 week <br> 1 week |
| ENDURING UNDERSTANDING |  | ESSENTIAL QUESTIONS |  |
| - Slope is a rate of change for a set of data or a linear graph. <br> - Linear functions are defined by constant slope. <br> - Collecting and examining data can sometimes help one discover patterns in the way in which two quantities vary. <br> - Written descriptions, tables, graphs, and equations are useful in representing and investigating relationships between varying quantities. <br> - Different representations (written descriptions, tables, graphs, and equations) of the relationships between varying quantities may have different strengths and weaknesses. <br> - Solving problems involving linear relationships requires gathering data. <br> - A scatter plot's best fit line is used to make predictions for data not on the line or table. <br> - Memorizing formulas aids in efficient problem solving. |  | - For a given set of data or a graph, how can units of measurement help us explain the meaning of slope? <br> - What are the different ways to graph linear equations? <br> - How do coordinate graphs demonstrate solutions and non-solutions of equations with two variables? <br> - What does the graphical data tell me? <br> - What is the relationship between the $x$ - and $y$-axis in any given situation? <br> - How does a change in one variable affect the other variable in a given situation? <br> - Which tells me more about the relationship I am investigating - a table, a graph, or an equation? Why? <br> - What strategies can I use to help me understand and represent real situations involving linear relationships? <br> - How will applying appropriate measurement techniques, tools, and formulas help solve geometric problems efficiently? <br> - How does fluency with formulas improve accuracy and speed in solving problems? |  |
| Differentiation and Accommodations |  | District/School Primary and Supplementary Resources |  |
| - Provide graphic organizers <br> - Provide additional examples and opportunities for additional problems |  | - Prentice Hall Course 3 Mathematics Common Core Textbook <br> - IXL |  |
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for repetition

- Provide tutoring opportunities
- Provide retesting opportunities after remediation (up to teacher and district discretion)
- Teach for mastery not test
- Teaching concepts in different modalities
- Adjust pace and homework assignments


## Instructional Strategies

Fairfield Township School recognizes the importance of the varying methodologies that may be successfully employed by teachers within the classroom and, as a result, identifies a wide variety of possible instructional strategies that may be used effectively to support student achievement. These may include, but not be limited to, strategies that fall into categories identified by the Framework for Teaching by Charlotte Danielson:

- Communicating with students
- Using questioning and discussion techniques
- Engaging students in learning
- Using assessment in instruction
- Demonstrating Flexibility and Responsiveness

| Common Misconceptions | Proper Conceptions |
| :--- | :--- |
|  |  |
| Students confuse the $x$-axis and the $y$-axis. | The $x$-axis is horizontal and the y-axis is vertical. |
| Students confuse positive, negative, and no correlations | Positive correlations rise from the left to the right. Negative correlations decline <br> from the left to the right. No correlations are scattered. |

## Performance Task

The class will participate in a survey during which each student will tell their height and shoe size.

- Students will record this data in a table.
- Students will use this data to construct a scatter plot.
- Students will title their scatter plot and label the axes.
- Students will explain what type of correlation is shown in their scatter plot.


## Rubric

When used as a quiz grade (based on 100\%), each bullet would be worth 25 points for a correct answer.
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